

**CASE WESTERN RESERVE UNIVERSITY**  
 Case School of Engineering  
 Department of Electrical Engineering and Computer Science  
**ENGR 210. Introduction to Circuits and Instruments (4)**

**FORMULA SHEET**

TRIG IDENTITIES:

$$\cos(x + y) = \cos x \cos y - \sin x \sin y \qquad \sin(x + y) = \sin x \cos y + \cos x \sin y$$

$$\sin(2x) = 2 \sin x \cos x \qquad \cos(2x) = 2 \cos^2 x - 1 = 1 - 2 \sin^2 x$$

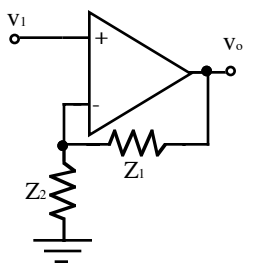
FOURIER COEFFICIENTS:  $v(t) = V_A \cos(\omega t + \phi) = a \cos(\omega t) + b \sin(\omega t)$  where

$$V_A = \sqrt{a^2 + b^2} \text{ and } \phi = \tan^{-1} \frac{b}{a}. \text{ Conversely, } a = V_A \cos \phi \text{ and } b = V_A \sin \phi$$

|                       | INDUCTORS                 | CAPACITORS                  |
|-----------------------|---------------------------|-----------------------------|
| Terminal relationship | $v_L = L \frac{di_L}{dt}$ | $i_C = C \frac{dv_C}{dt}$   |
| Impedance             | $Z_L = j\omega L$         | $Z_C = \frac{1}{j\omega C}$ |
| Time constant         | $T_C = \frac{L}{R_T}$     | $T_C = R_T C$               |

INITIAL/FINAL VALUE THEOREM:  $f(t) = [IV - FV]e^{-\frac{t}{T_C}} + FV$   
 where IV=initial value and FV=final value.

OP AMP CIRCUITS:

| CIRCUIT   | BLOCK DIAGRAM  | GAINS                       |
|---|--|-----------------------------|
|  | $v_1 \rightarrow \boxed{K} \rightarrow v_o$<br><br>Non-inverting amplifier | $K = \frac{Z_1 + Z_2}{Z_2}$ |

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|  |  |   |
|--|--|---|
|  | <p style="text-align: center;">Inverting amplifier</p> | $K = -\frac{Z_2}{Z_1}$  |
|  | <p style="text-align: center;">Summer</p>              | $K_1 = -\frac{Z_F}{Z_1}, \quad K_2 = -\frac{Z_F}{Z_2}$  |
|  | <p style="text-align: center;">Subtractor</p>          | $K_1 = -\frac{Z_2}{Z_1}, \quad K_2 = \left(\frac{Z_1 + Z_2}{Z_1}\right) \left(\frac{Z_4}{Z_3 + Z_4}\right)$ |
|  | <p style="text-align: center;">Integrator</p>          | $K = -\frac{1}{RC}$   |
|  | <p style="text-align: center;">Differentiator</p>      | $K = -RC$   |